



Probing relatively heavier right-handed selectron at the CEPC, FCC_{ee} and ILC

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ABSTRACT

We employ the low energy Minimal Supersymmetric Standard Model (MSSM) to explore the parameter space associated with Z-pole and Higgs-pole solutions. Such parameter spaces can not only saturate the cold dark matter relic density bound within 5σ set by the Planck 2018, but also satisfy the other standard collider mass bounds and B-physics bounds. In particular, we show that the right-handed selectron can be light. Thus, we propose a search for the relatively heavier right-handed selectron at the future lepton colliders with the center-of-mass energy $\sqrt{s} = 240$ GeV and integrated luminosity 3000 fb^{-1} via the mono-photon channel: $e_R^+ e_R^- \rightarrow \tilde{\chi}_1^0(\text{bino}) + \tilde{\chi}_1^0(\text{bino}) + \gamma$. We show that for the Z-pole case the right-handed selectron will be excluded up to 180 GeV and 210 GeV respectively at 3σ and 2σ , while the right-handed selectron will be excluded up to 140 GeV and 180 GeV respectively at 3σ and 2σ in case of Higgs-pole.

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1. Introduction

Despite the fact that the Supersymmetric Standard Models (SSMs) are the best bet for the new physics beyond the standard model (BSM) but no concrete evidence has been found. The SSMs predict the unification of the gauge couplings of the hypercharge (or say electromagnetic), weak and strong interactions [1–6], provide the natural solution to gauge hierarchy problem, and have the lightest supersymmetric particle (LSP) as a fine cold dark matter candidate [7,8]. It is also interesting to note that the minimal SSM (MSSM) also predicts the mass range of the Higgs boson [100,135] GeV [9]. This is why Supersymmetry (SUSY) has been one of the main targets of the searches being done to look for the BSM physics at the Large Hadron Collider (LHC). Despite all the efforts at the end of the LHC Run-2 and accumulating data of about 140 fb^{-1} at the center of mass (CM) energy 13 TeV, we have no obvious signal of SUSY. The LHC SUSY searches have put strong constraints on the SSMs. For instance, the masses of the gluino, first-two generation squarks, stop, and sbottom must be larger than about 2.3 TeV, 1.9 TeV, 1.25 TeV, and 1.5 TeV, respec-

tively [10–14]. Thus, at least the colored supersymmetric particles (sparticles) must be heavier about TeV scale.

To escape the LHC SUSY search constraints but remain consistent with various experimental results, one proposed the Electroweak Supersymmetry (EWSUSY) [15–17], where the squarks and/or gluinos are around a few TeV while the sleptons, sneutrinos, Bino and Winos are within about 1 TeV. The Higgsinos (or say the Higgs bilinear μ term) can be either heavy or light. Especially, the EWSUSY can be realized in the Generalized Minimal Supergravity (GmSUGRA) [18,19].

In parallel to high energy hadron collider experiments for the BSM physics, high energy physics community also have plans to build lepton colliders such as Circular Electro-Positron Collider (CEPC) in China [20,21], Future Circular Collider (FCC_{ee}) at CERN [22,23], and International Linear Collider (ILC) [24,25]. We know that in lepton collider such as e^+e^- , initial states are well defined (E, p) with known polarization and less background particles are produced after collision. They are ideal machines for high-precision measurements. If we take CEPC as an example, it is a collider with a circumference of 100 km which is designed to operate at center-of-mass energy $\sqrt{s} = 240$ GeV, 91.2 GeV, and around 160 GeV as Higgs factory, Z factory or Z-pole and $W - W$ threshold scan respectively. It will produce large samples of Higgs, W and Z

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bosons to allow precision measurements of their properties as well as searches for the BSM physics.

The interesting question is whether we can probe the relatively heavy sparticles at the future lepton colliders. In this paper, we study the EWSUSY parameter space under the low scale MSSM boundary conditions. Especially, we have the Z-pole ($m_{\tilde{\chi}_1^0} \approx 1/2m_Z$) and Higgs-pole ($m_{\tilde{\chi}_1^0} \approx 1/2m_h$) solutions where $m_{\tilde{\chi}_1^0}$ is the Bino-like LSP neutralino mass. These solutions satisfy the Higgs mass bounds, B-physics bounds, and sparticle mass bounds, and have the correct cold dark matter relic density given by Planck 2018. Of course, we do have some fine-tuning for these solutions. However, to explain the observed dark matter density for the LSP neutralino in the SSMs naturally, we only have the bulk region with small values of m_0 and $m_{1/2}$, where the neutralino pair annihilation occurs at a large rate via t -channel slepton exchange. However, this region has already been ruled out by the LHC experiments. Thus, in general, we always need some fine-tuning to obtain the correct dark matter density, for example, Higgs/Z poles, and various coannihilation scenarios, etc. Moreover, we present a few benchmark points to show the parameter space. In addition to it, making the most of the opportunity of the Z-pole and Higgs-pole parameter space, for the first time we propose a new search for the relatively heavier right-handed selectron at future lepton colliders with the center-of-mass energy $\sqrt{s} = 240$ GeV and integrated luminosity 3000 fb^{-1} via mono-photon channel: $e^+e^- \rightarrow \tilde{\chi}_1^0(\text{bino}) + \tilde{\chi}_1^0(\text{bino}) + \gamma$. In this analysis, we consider $e_R^+e_R^- \rightarrow \nu\bar{\nu}\gamma$ as the SM background and neglect the events involving $W^\pm$ as mediator due to the right-handed selectron search. We find that for the Z-pole case, the right-handed selectron can be excluded up to 180 GeV and 210 GeV at 3σ and 2σ , respectively, while the right-handed selectron will be excluded up to 140 GeV and 180 GeV at 3σ and 2σ in case of Higgs pole, respectively. However, the viable parameter space, which we present here, does not contribute significantly to the muon anomalous magnetic moment [26].

The rest of the paper is organized as follows. We describe the input parameter and the ranges for scan in section 2. We display results of scans in section 3 and discuss our collider study in section 4. Finally we conclude in section 5.

2. Scanning procedure and phenomenological constraints

We employ SPheno 4.0.3 package [27,28] that is generated with SARAH 4.13.0 [29,30] to perform the focused scan and explore the parameter space having Z-resonance and Higgs-resonance solutions. During our focused scan, we adopted the following (universality) conditions to impose on the parameter space of the MSSM at the EW scale:

$$M_{\tilde{f}} \equiv M_{Q_{1,2,3}} = M_{U_{1,2,3}} = M_{D_{1,2,3}},$$

$$T_{\tilde{f}} \equiv T_{\tilde{t}} = T_{\tilde{b}} = T_{\tilde{\tau}},$$

where $M_{Q_{1,2,3}}^2$, $M_{U_{1,2,3}}^2$ and $M_{D_{1,2,3}}^2$ are the squared soft masses of the sfermions. The parameter $T_{\tilde{f}}$ corresponds to sfermion trilinear couplings; usually these are taken to be proportional to the Yukawas, such that $T_{\tilde{f}}^{ij} = Y_{ij}^f A_{\tilde{f}}$, where i, j are generation indices. In our numerical code, we fixed all the elements of $T_{\tilde{f}}$ to small values (1 GeV for the diagonal terms and zero otherwise), except for $T_{\tilde{f}}^{(3,3)} = T_{\tilde{t}}^{(3,3)} = T_{\tilde{b}}^{(3,3)} = T_{\tilde{\tau}}^{(3,3)}$, which we left as a free parameter to be scanned over an extended range. We also consider non-universal gauginos and slepton masses to generate the particle spectrum for a given configuration of the final set of the free parameters,

$$M_1, M_2, M_3, T_{\tilde{f}}, \tan\beta, M_{\tilde{f}}, m_A, \mu, M_{L_{1,2,3}}^2, M_{E_{1,2,3}}^2$$

In order to calculate $\Omega_{\tilde{\chi}_1^0} h^2$ and other DM observables for each sampled parameter space point, we also produce a CalcHEP [31] model file for the MSSM with SARAH, which is then embedded in the public code MicrOmegas-v5.2.4 [32–34].

In scanning the parameter space, we use the SSP [35] Mathematica package and link with SPheno and MicrOmegas. The data points collected all satisfy the requirement of REWSB, with the neutralino being the LSP. After collecting the data, we require the following bounds (inspired by the LEP2 experiment) on sparticle masses.

LEP constraints: We impose the bounds that the LEP2 experiments set on charged sparticle masses ($\gtrsim 100$ GeV) [36].

Higgs Boson mass: The experimental combination for the Higgs mass reported by the ATLAS and CMS Collaborations is [37]

$$m_h = 125.09 \pm 0.21(\text{stat.}) \pm 0.11(\text{syst.}) \text{ GeV}. \quad (2.1)$$

Due to the theoretical uncertainty in the Higgs mass calculations in the MSSM – see e.g. [38,39] – we apply the constraint from the Higgs boson mass to our results as:

$$122 \text{ GeV} \leq m_h \leq 128 \text{ GeV}. \quad (2.2)$$

Rare B-meson decays: Since the SM predictions are in a good agreement with the experimental results for the rare decays of B-meson such as the $B_s \rightarrow \mu^+\mu^-$, $B_s \rightarrow X_s\gamma$, where X_s is an appropriate state including a strange quark, the results of our analyses are required to be consistent with the measurements for such processes. Thus we employ the following constraints from B-physics [40,41]:

$$1.6 \times 10^{-9} \leq \text{BR}(B_s \rightarrow \mu^+\mu^-) \leq 4.2 \times 10^{-9}, \quad (2.3)$$

$$2.99 \times 10^{-4} \leq \text{BR}(b \rightarrow s\gamma) \leq 3.87 \times 10^{-4}, \quad (2.4)$$

$$0.70 \times 10^{-4} \leq \text{BR}(B_u \rightarrow \tau\nu_\tau) \leq 1.5 \times 10^{-4}. \quad (2.5)$$

Current LHC searches: Based on [42–44], we consider the following constraints on gluino and first/second generation squark masses

$$(a) \quad m_{\tilde{g}} \gtrsim 2.2 \text{ TeV}, \quad m_{\tilde{q}} \gtrsim 2 \text{ TeV}, \quad (2.6)$$

DM searches and relic density: For the discussion on the phenomenology of neutralino DM in our scenario, we impose the following constraint for the LSP relic density, based on the current measurements of the Planck satellite [45]:

$$0.114 \leq \Omega_{\text{CDM}} h^2 (\text{Planck2018}) \leq 0.126 (5\sigma). \quad (2.7)$$

We use the current XENON1T with $2 \cdot y$ spin-independent (SI) DM cross section with bounds [46]. All points lying above these upper bounds have been excluded from the plots.

3. Results of focused scans

In this section we are focusing on the sparticle spectrum consistent with mass bounds and the constraints discussed above.

In Fig. 1, we display plots in $m_{\tilde{\chi}_1^0} - m_{\tilde{e}_1}$ and $m_{\tilde{\chi}_1^0} - m_{\tilde{e}_2}$ planes. Note that here $\tilde{e}_1$ is the right-handed selectron and $\tilde{e}_2$ is the left handed selectron. Gray points satisfy the REWSB and the LSP neutralino conditions. Green points satisfy the mass bounds and B-physics constraints. Red points form a subset of green points and satisfy the Planck 2018 bounds (mentioned above) on the relic abundance of the LSP neutralino within 5σ uncertainty. We see that from left panel the green points are almost everywhere. But

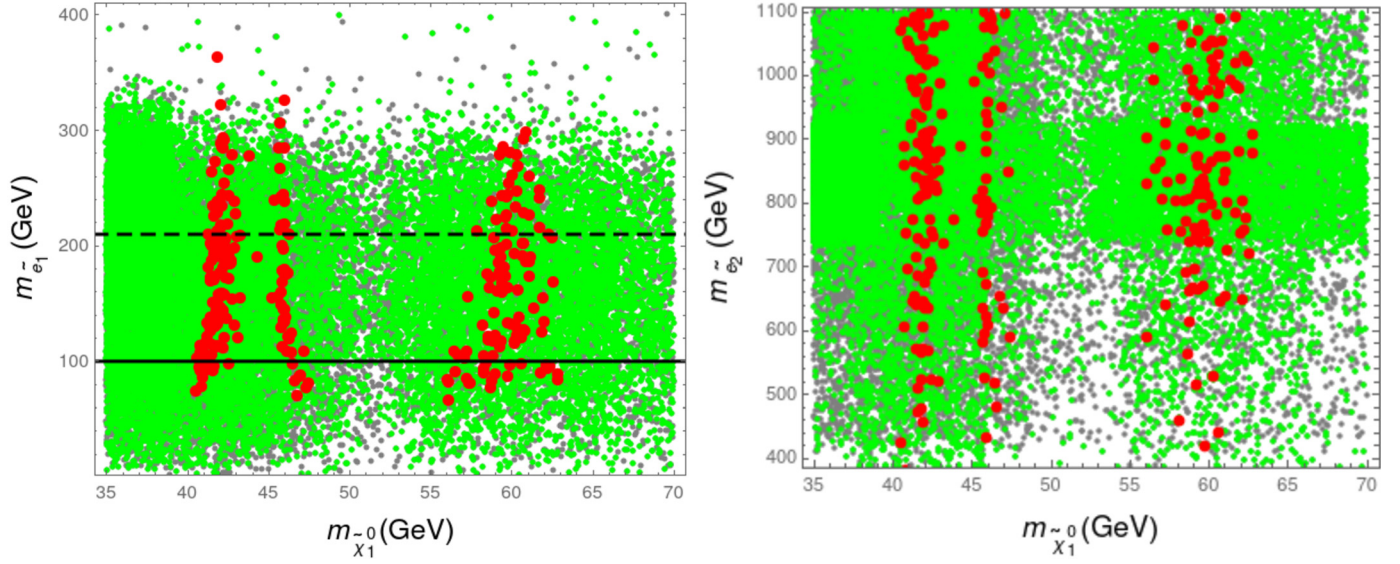


Fig. 1. Parameter spaces in the $m_{\tilde{\chi}_1^0} - m_{\tilde{e}_1}$ and $m_{\tilde{\chi}_1^0} - m_{\tilde{e}_2}$ planes. Gray points are consistent with the REWSB and LSP neutralino. Green points satisfy the mass bounds including $m_h = 125 \pm 3$ GeV and the constraints from rare B -meson decays. Red points form a subset of green points and satisfy the 5σ Planck bounds on dark matter relic density.

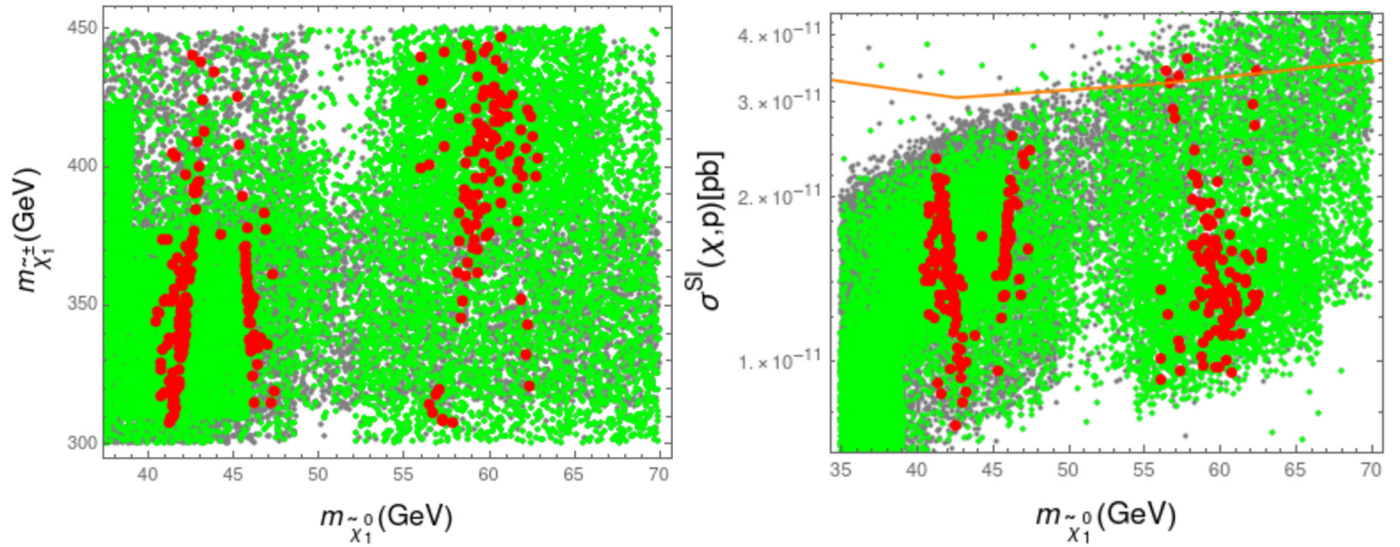


Fig. 2. Parameter spaces in the $m_{\tilde{\chi}_1^0} - m_{\tilde{\chi}_1^\pm}$ and $m_{\tilde{\chi}_1^0} - \sigma^{SI}(\chi, p)$ planes. Color coding is same as in Fig. 1.

when we demand the relic density bound, red solutions appear to be around $m_{\tilde{\chi}_1^0} \sim 45$ GeV or 62 GeV. These solutions represent the well-known Z-pole ($m_{\tilde{\chi}_1^0} \approx 1/2 m_Z$) and the Higgs-pole ($m_{\tilde{\chi}_1^0} \approx 1/2 m_h$) solutions where two LSP neutralinos annihilate via s-channel exchange of a virtual particle, for example, a Z or Higgs boson and the mass of the exchanged particle matches twice the LSP neutralino mass closely. The solid black horizontal line indicates the LEP bounds on sleptons [47–51] while the dashed black line represents the estimated exclusion limit for right handed selectron (we will discuss it in section 4). Note that though red points appear to be between 80 GeV to 360 GeV in our present scans but we can increase the mass range by repeating focus scans. In the left panel we see the similar situation for neutralino mass and we note that $\tilde{e}_2$ or the left handed slepton mass can be as heavy as 1100 GeV.

In the left panel of Fig. 2, we show plots for $m_{\tilde{\chi}_1^0} - m_{\tilde{\chi}_1^\pm}$ and $m_{\tilde{\chi}_1^0} - \sigma^{SI}(\chi, p)$. Color definition is same as in Fig. 1. In the left

panel we can see that $m_{\tilde{\chi}_1^\pm}$ can be as heavy as 450 GeV for both Z-pole and Higgs-pole scenario but can be made heavy by focused scans. The right panel displays $m_{\tilde{\chi}_1^0} - \sigma^{SI}(\chi, p)$ plot. The orange line represents the current XENON1T with $2 t \cdot y$ [46] bounds. In this plot, the two dips around 45 GeV and 62 GeV indicate the Z-pole and Higgs-pole solutions. This plot clearly shows that almost all of the red points are consistent with the current bounds set by XENON1T with $2 t \cdot y$ [46].

In order to show the glimpse of the parameter space we display four benchmark points. Point 1 and Point 2 are examples of Z-pole solutions and Point 3 and Point 4 display examples of Higgs-pole solutions (Table 1).

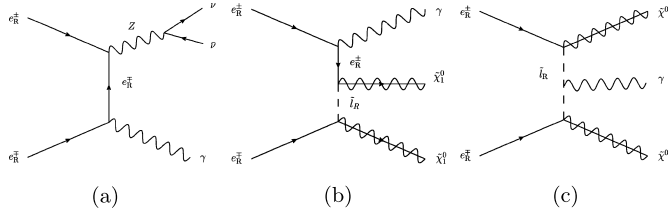
4. Collider analysis

In this section, we investigate the lepton collider approach to bino-like LSP via a light right-handed selectron. We study the final states with missing transverse energy induced by two bino-like

Table 1

The sparticle and Higgs masses (in GeV units) for the benchmark points.

	Point 1	Point 2	Point 3	Point 4
M_1	59.67	48.3	64.38	63.99
M_2	650.33	641.2	486.97	494.92
M_3	-3720.77	-2579.8	-3030	-4024
$M_{\tilde{f}}$	3299.84	3456.79	3083.03	3146.76
$m_{\tilde{t}}$	848.39	824.63	912.81	1005.25
$m_{\tilde{e}^c}$	371.121	340.65	323.66	379.464
T_f	-3793.68	-2597.75	-2952.52	-4429.96
$\tan \beta$	57.2	56.9	59.96	47.69
μ	318.24	339	361.1	440.6
m_h	125.5	123	124	127
m_H	4095.9	4000	3842	4093
m_A	4096	4000	3842	4093
$m_{H^\pm}$	4104.39	4041	3858	4102
$m_{\tilde{\chi}_{1,2}^0}$	57, 319	46, 339	62, 351	62, 391
$m_{\tilde{\chi}_{3,4}^0}$	330, 693	351, 684	373, 535	417, 548
$m_{\tilde{\chi}_{1,2}^\pm}$	319, 692	339, 684	352, 536	392, 549
$m_{\tilde{g}}$	3864	2872	3234	4087
$m_{\tilde{u}_{1,2}}$	3252, 3434	3422, 3542	3051, 3195	3059, 3283
$m_{\tilde{t}_{1,2}}$	3430, 3440	3542, 3552	3192, 3202	3274, 3288
$m_{\tilde{d}_{1,2}}$	3354, 3430	3475, 3543	3122, 3193	3197, 3275
$m_{\tilde{b}_{1,2}}$	3430, 3441	3543, 3553	3193, 3203	3275, 3285
$m_{\tilde{\nu}_1}$	799	785	875	1014
$m_{\tilde{\nu}_3}$	851	826	911	1054
$m_{\tilde{e}_{1,2}}$	102, 805	120, 791	125, 881	215, 1018
$m_{\tilde{\tau}_{1,2}}$	391, 855	364, 831	346, 915	400, 1057
$\sigma_{SI}(\text{pb})$	2.79×10^{-11}	1.72×10^{-11}	2.33×10^{-11}	1.38×10^{-11}
$\sigma_{SD}(\text{pb})$	1.33×10^{-5}	1×10^{-5}	8.18×10^{-6}	5.03×10^{-6}
$\Omega_{CDM} h^2$	0.116	0.118	0.1257	0.1259

**Fig. 3.** The Feynman diagrams for the background and signal events, respectively.

LSP plus an emissive mono-photon and focus on the t-channel process mediated by an off-shell right-handed slepton as shown in Fig. 3. In principle, such processes can probe slepton mass heavier than the collision energy. In order to further suppress the background events associated with W-boson process, we consider the polarized electron-positron collision with missing transverse energy induced by two neutralinos and an emissive mono-photon. The corresponding background events containing missing energy and mono-photon comes from Drell-Yan process with Z boson decay to two neutrinos.

In our numerical simulation, Monte Carlo samples of signal and background events are generated by using MadGraph5 [52,53] for hard scattering processes, PYTHIA8 [54] for parton showering and hadronization and DELPHES 3 [55] for jet clustering and detector simulation. We generate the signal events with the collision energy equal to 240 GeV and use the *anti* - k_T algorithm to do the jet reconstruction with the radius $R = 0.4$. The beam polarization is set to be fully right-handed. All jets and particles within $|\eta| < 3.0$ will be recorded by simulation, otherwise it will be missed. In addition, we apply photon isolation techniques, which have been developed to filter out indirect photons that are produced from the frag-

mentation of quark and gluon partons. Photon isolation viable is defined as

$$I(P) = \frac{\sum_{i \neq P}^{\Delta R < R_0, p_T^i > p_T^{min}} p_T(i)}{p_T(P)}, \quad (4.1)$$

where the denominator stands for the transverse momentum of photon, and the numerator is the sum of transverse momenta above p_T^{min} of all particles that lie within a cone of radius R_0 around and except the photon. In our simulation, we require the isolation viable to be $I(P) < 0.12$ and $R_0 = 0.5$, $p_T^{min} = 0.5$ GeV.

The final states is quite simple with only MET and mono-photon to be detected. Therefore, in order to analyze the signal events, we make use of the following quantities and the threshold is chosen to maximize the Higgs signal significance of the CEPC:

- Missing transverse energy (MET) of all invisible particles: We require $\cancel{E}_{inv} < 80.0$. The distribution of MET is shown in the left panel of Fig. 4, where the green region stands for the background distribution and the blue/orange one stands for the Higgs-pole case with slepton mass equal to 100 and 140 GeV respectively.
- Invariant mass of invisible particles:

$$m_{inv} = \sqrt{(E_{total} - E_{vis})^2 - p_{vis}^2},$$

where $E_{total} = 240$ GeV, E_{vis} the total energy of all visible particles and p_{vis} the visible particles. It should satisfy: $m_{inv} > 130.0$ GeV. Since for background events, two neutrinos come from an on-shell Z boson, so the invariant mass of two neutrinos is around Z boson mass as shown in the right panel in Fig. 4. In this panel, the color meaning is same as before, and as we can see, the distribution of Z-pole mass set an effective cut-off between signal events and background events.

Note that here we show our study for Higgs-pole only but more or less similar results true for Z-pole solutions.

Significance for signal events is calculated by $\sigma = S/\sqrt{B}$. In Fig. 5, we show the significance of signal events with the selectron mass ranging from 50 GeV to 400 GeV. For the Z-pole case, the right handed selectron will be excluded to 180 GeV and 210 GeV by 3σ and 2σ respectively. In the Higgs-pole scenario, the right handed selectron will be excluded to 140 GeV and 180 GeV by 3σ and 2σ respectively.

5. Discussion and conclusion

In the low energy MSSM, we studied the EWSUSY parameter space associated with Z-pole and Higgs-pole solutions. Such parameter spaces can not only have the correct dark matter relic density within 5σ from the Planck 2018, but also escape the other standard collider mass bounds and B-physics bounds. Especially, the right-handed selectron can be light. Therefore, we proposed a search for the relatively heavier right-handed selectron at the future lepton colliders with the center-of-mass energy $\sqrt{s} = 240$ GeV and integrated luminosity 3000 fb^{-1} via mono-photon channel: $e_R^+ e_R^- \rightarrow \tilde{\chi}_1^0(\text{bino}) + \tilde{\chi}_1^0(\text{bino}) + \gamma$. We showed that for the Z-pole case the right-handed selectron can be excluded up to 180 GeV and 210 GeV respectively at 3σ and 2σ , while the right-handed selectron can be excluded up to 140 GeV and 180 GeV respectively at 3σ and 2σ in case of Higgs-pole.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

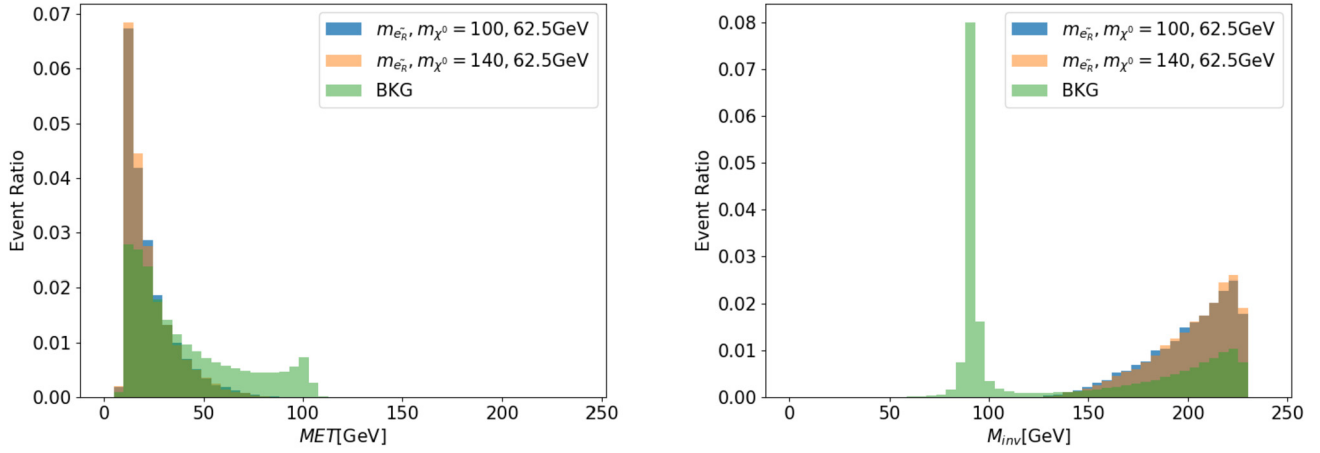


Fig. 4. The distribution of missing transverse momentum (left) and the invariant mass of the missing momentum (right) for Higgs-pole case with $m_{\tilde{e}_R} = 100$ GeV and $m_{\tilde{e}_R} = 140$ GeV.

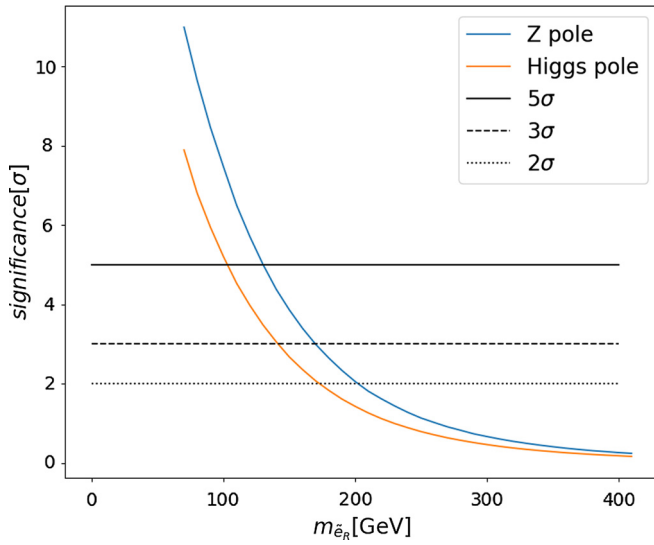


Fig. 5. Significance of exclusion ability.

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